

```

> with(DEtools):
> phug:=[ D(theta)(t) = v(t) - cos(theta(t))/v(t),
  D(v)(t)      = -sin(theta(t)) -R*v(t)^2];
  phug := 
$$\left[ D(\theta)(t) = v(t) - \frac{\cos(\theta(t))}{v(t)}, D(v)(t) = -\sin(\theta(t)) - R v(t)^2 \right] \quad (1)$$

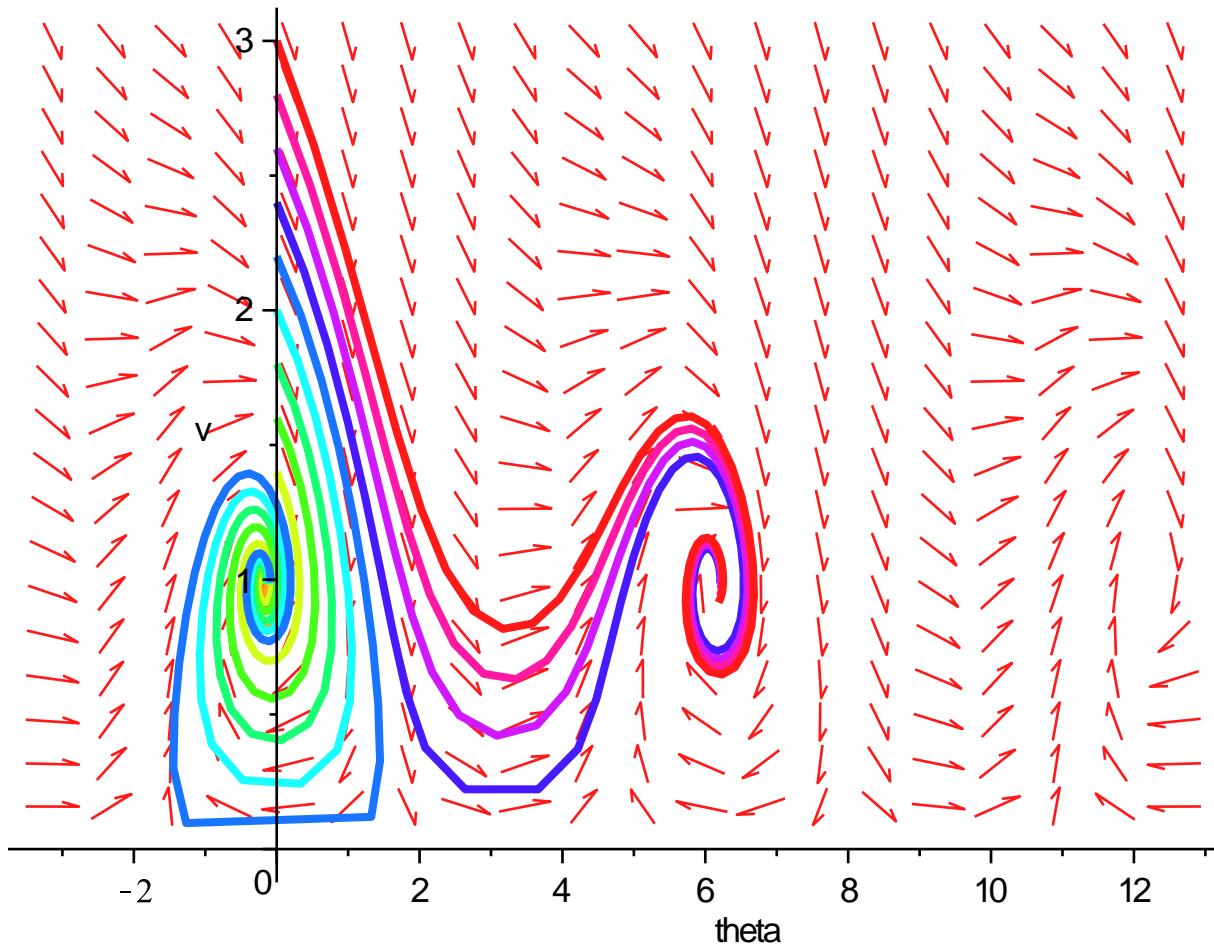

```

```

> R:=.2;
phase2:=DEplot( phug, [theta(t), v(t)], t=0..10,
  theta=-Pi..4*Pi, v=0..3,
  [seq([theta(0)=0, v(0)=i], i=1..3, 0.2)],
  linecolor=[seq(COLOR(HUE,i), i=0..1,.1)]);
phase2;

```

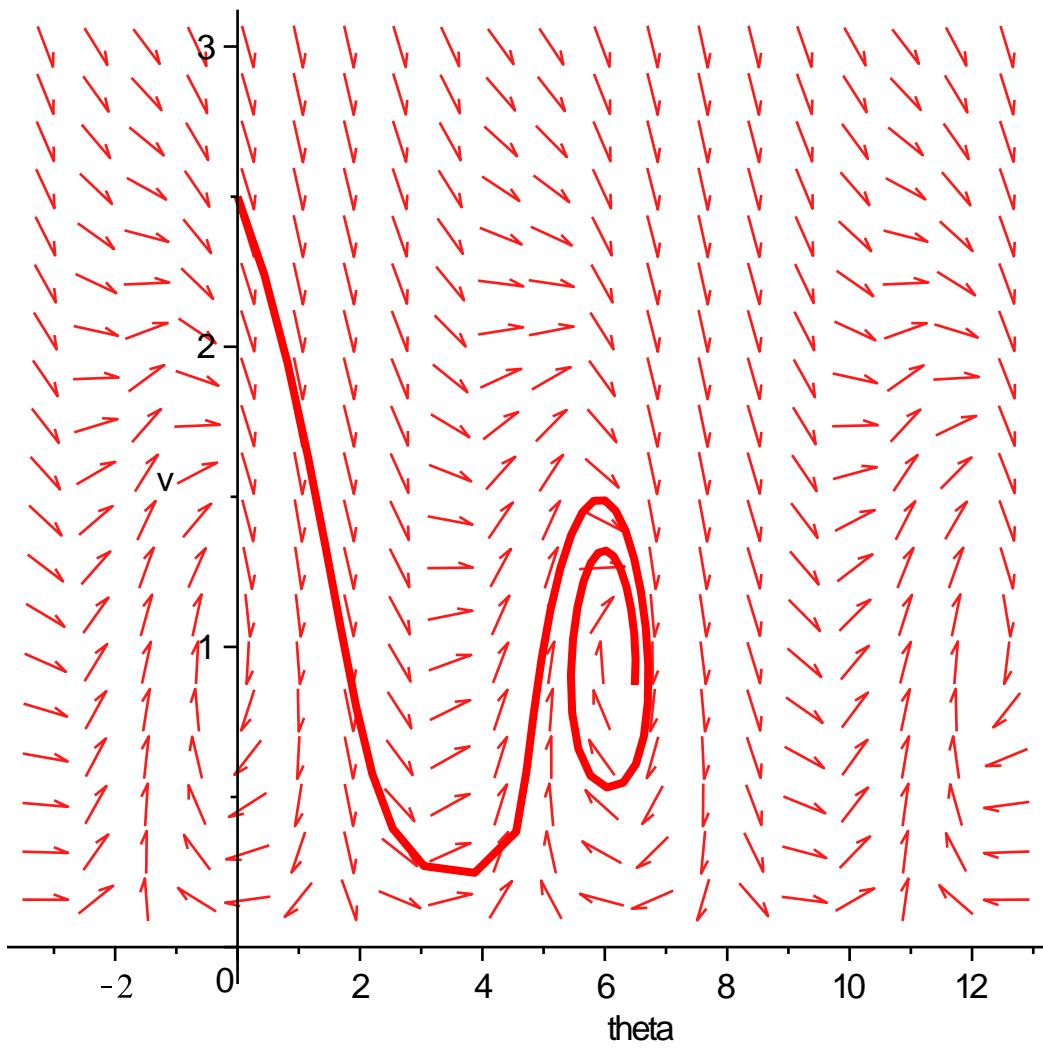
$R := 0.2$   
 $phase2 := PLOT(\dots)$



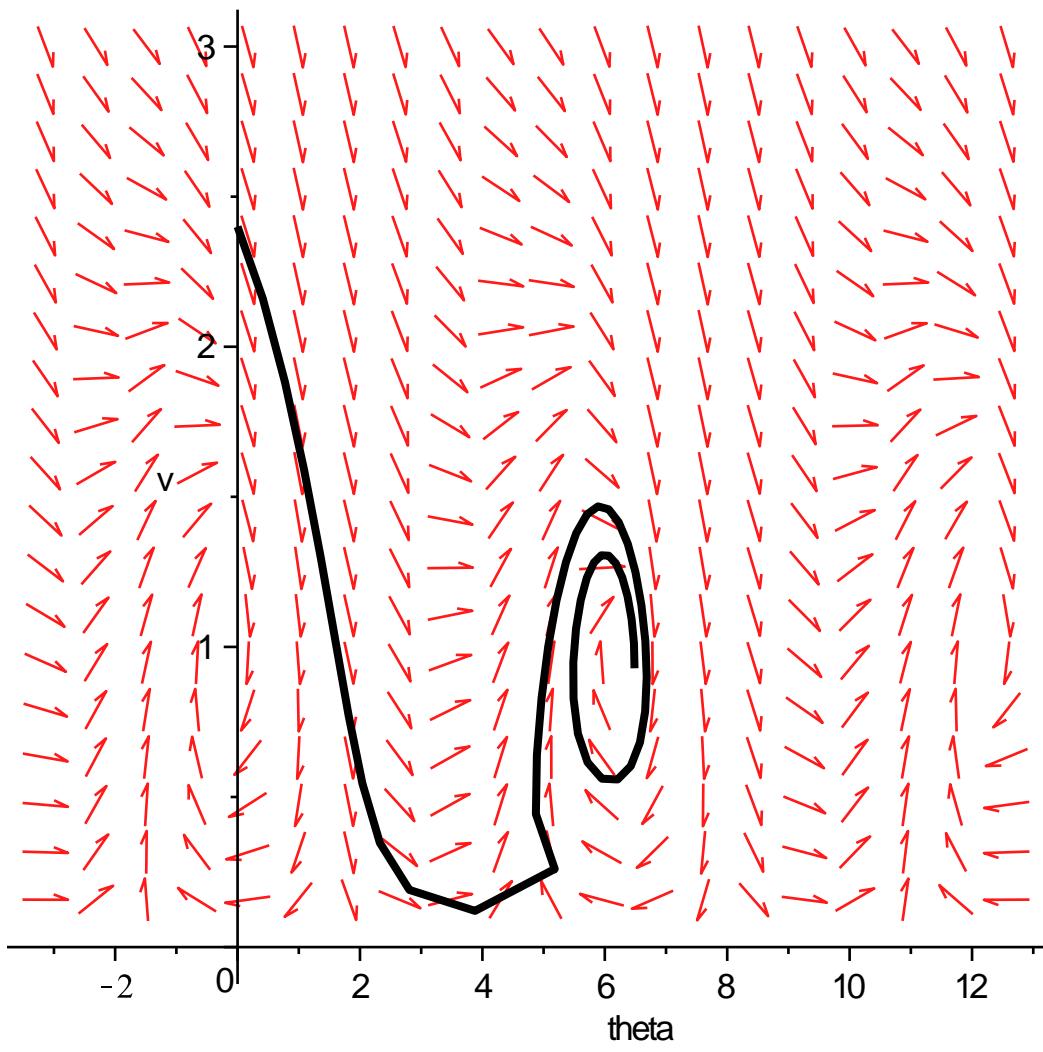
```

> DEplot( phug, [theta(t), v(t)], t=0..10,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=2.5]],
  linecolor=[red], method=classical[froeuler]);

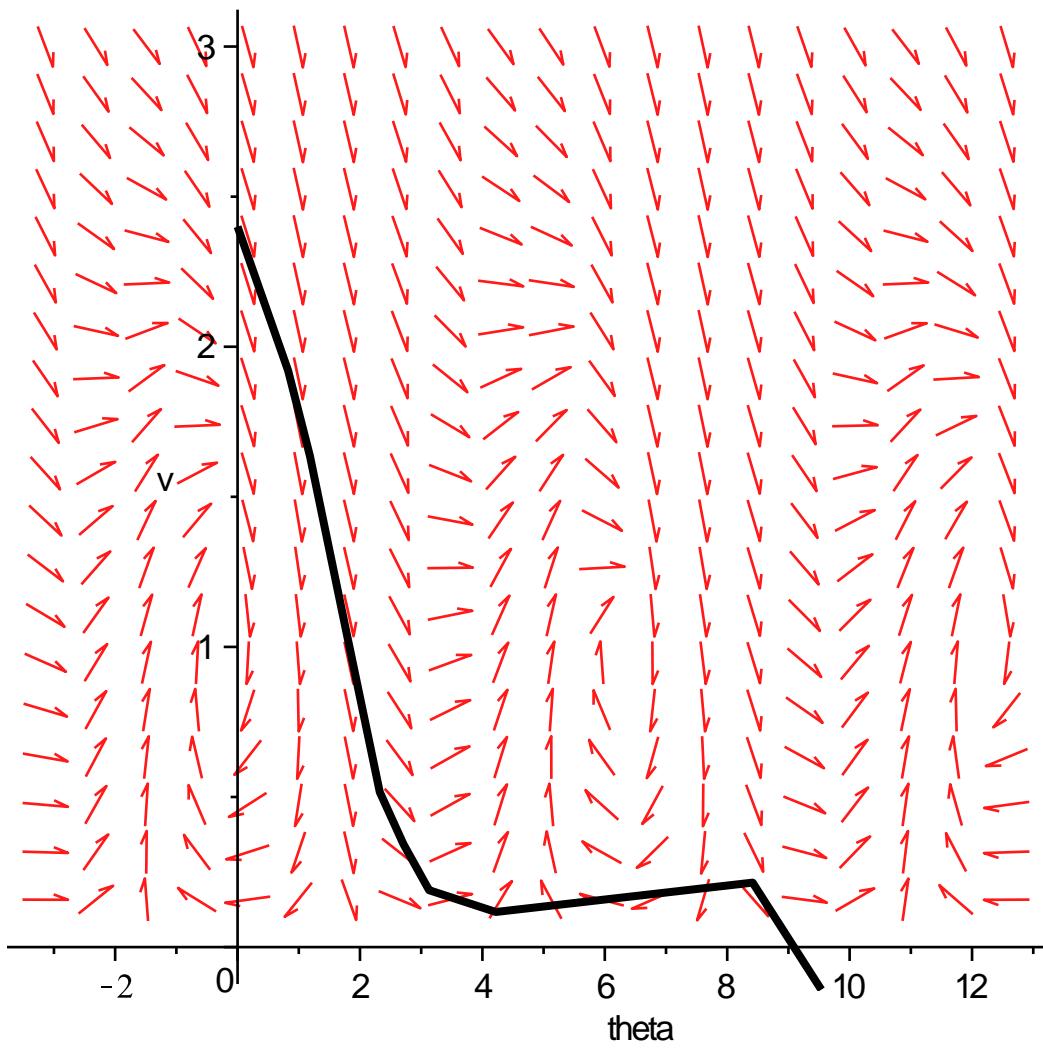
```



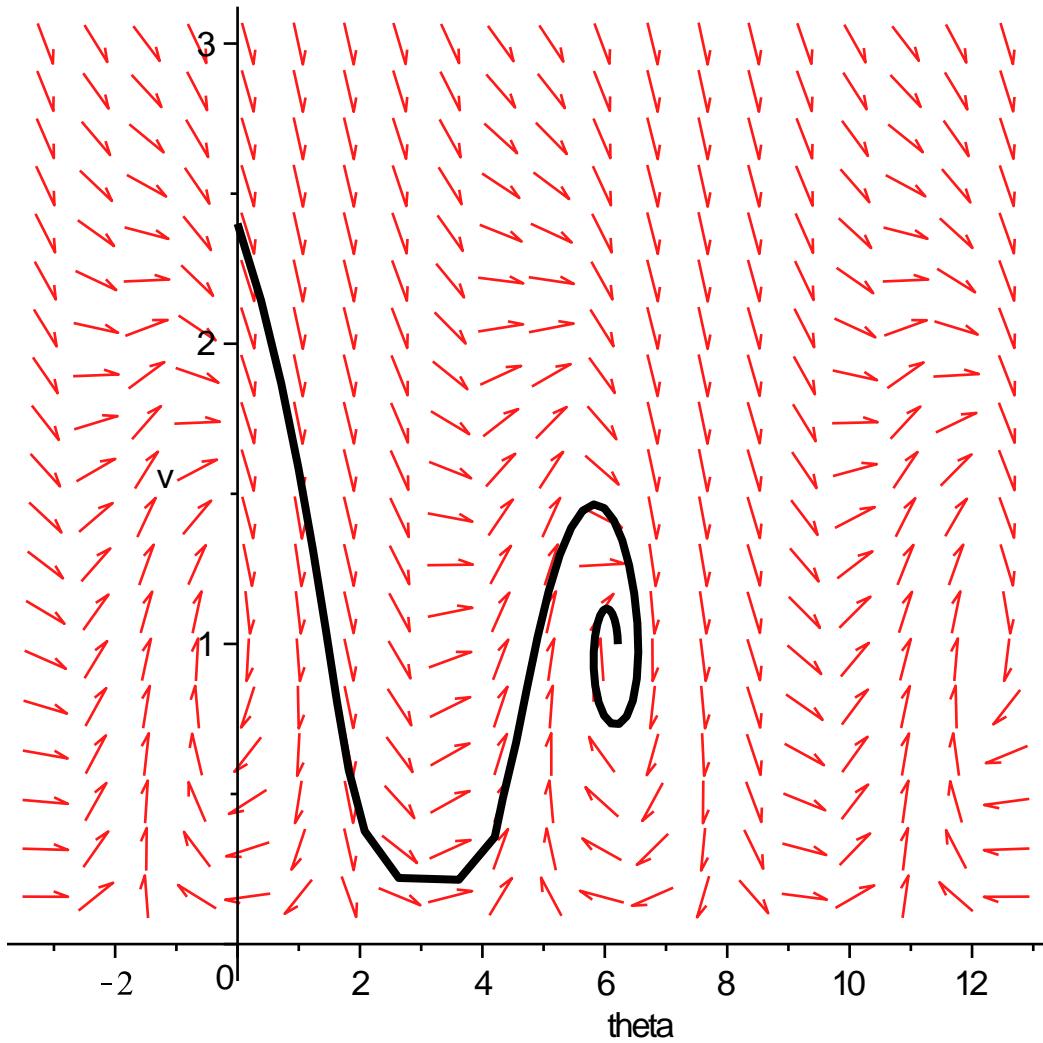
```
> DEplot( phug, [theta(t), v(t)], t=0..10,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=2.4]],
  [linecolor=[black], method=classical[foreuler]]);
```



```
> DEplot( phug, [theta(t), v(t)], t=0..10,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=2.4]],
  linecolor=[black], method=classical[foreuler], stepsize=1/2);
```



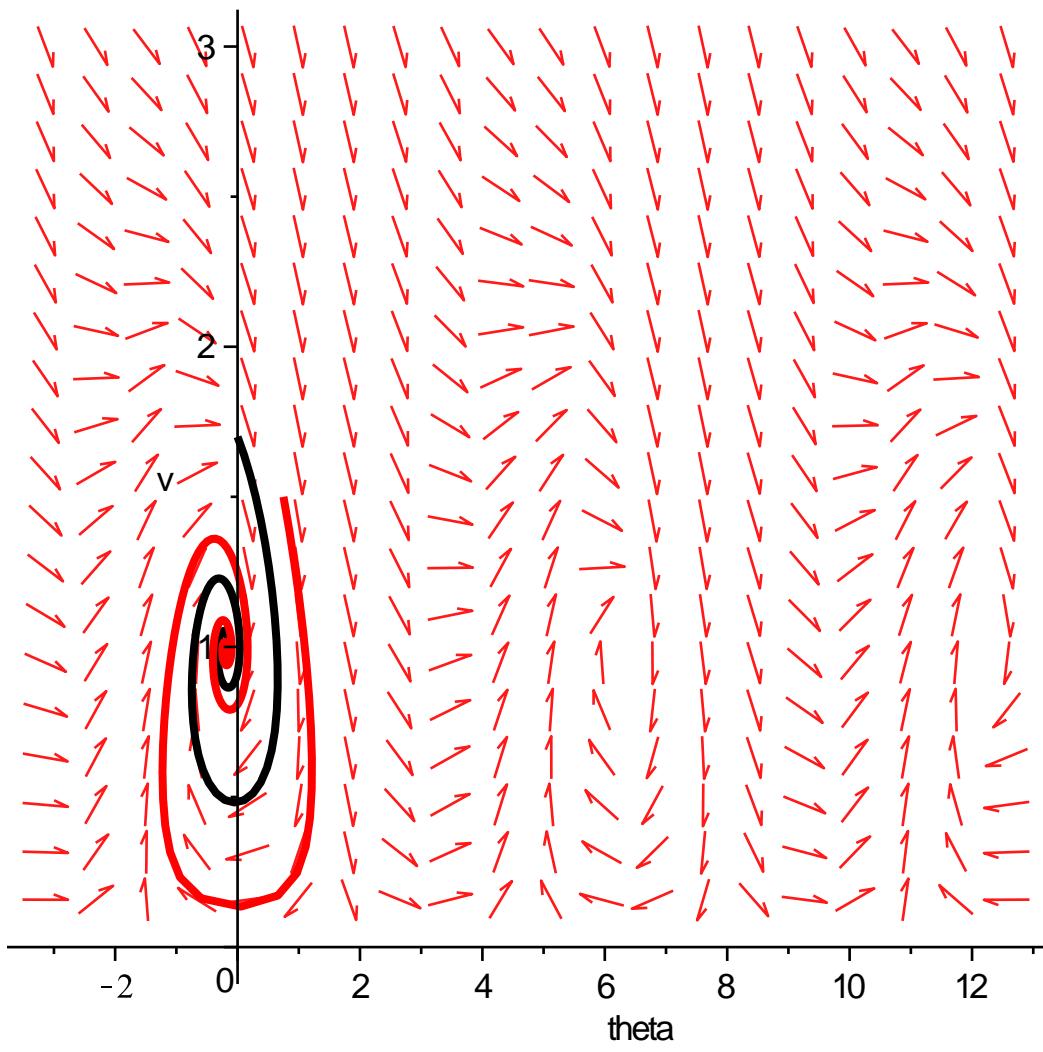
```
> DEplot( phug, [theta(t), v(t)], t=0..10,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=2.4]],
  linecolor=[black], method=classical[rk4], stepsize=1/2);
```



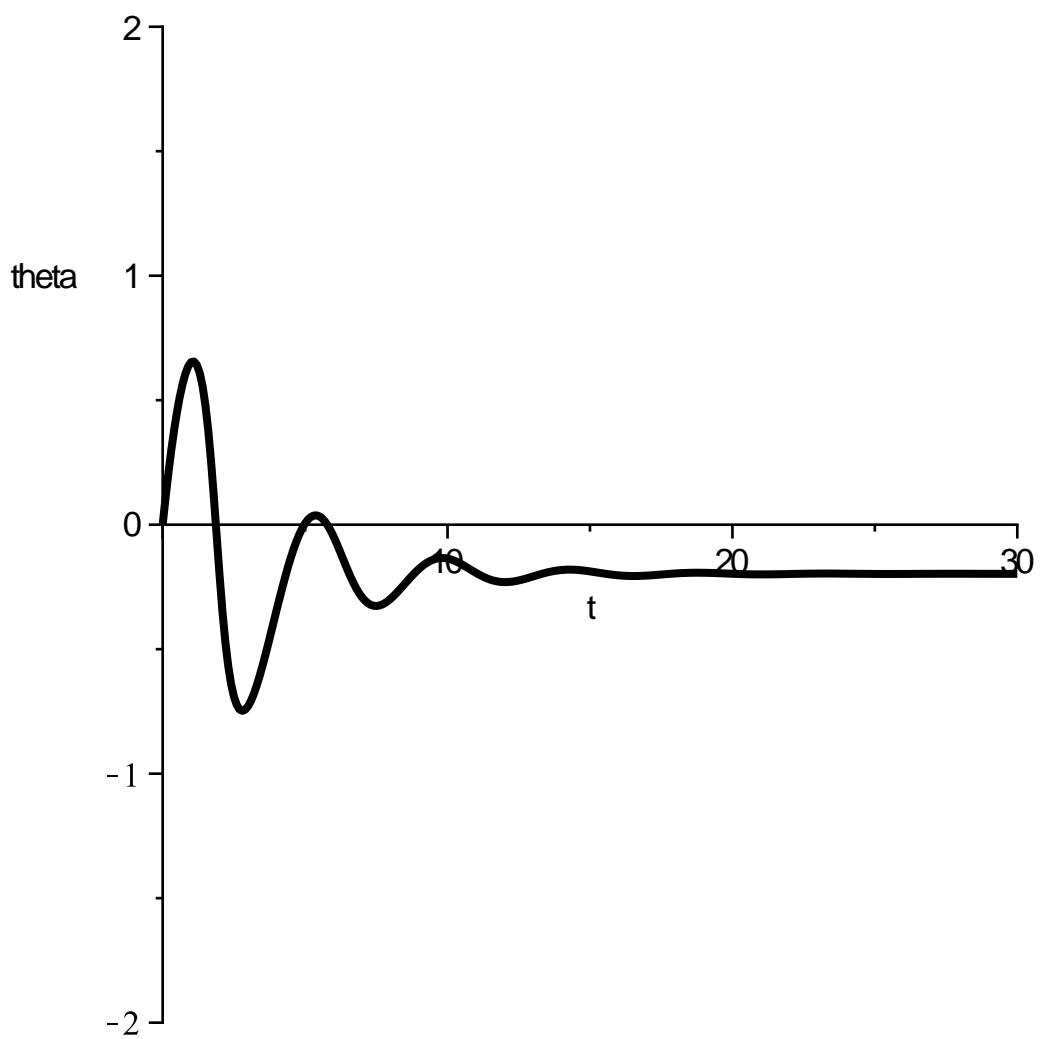
```

> DEplot( phug, [theta(t), v(t)], t=0..10,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=2.4]],
  linecolor=[black], method=classical[rk4], stepsize=0.00001);
Warning. computation interrupted
> DEplot( phug, [theta(t), v(t)], t=0..20,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=1.7],[theta(0)=.75, v(0)=1.5]], stepsize=
  0.1,
  linecolor=[black, red]);

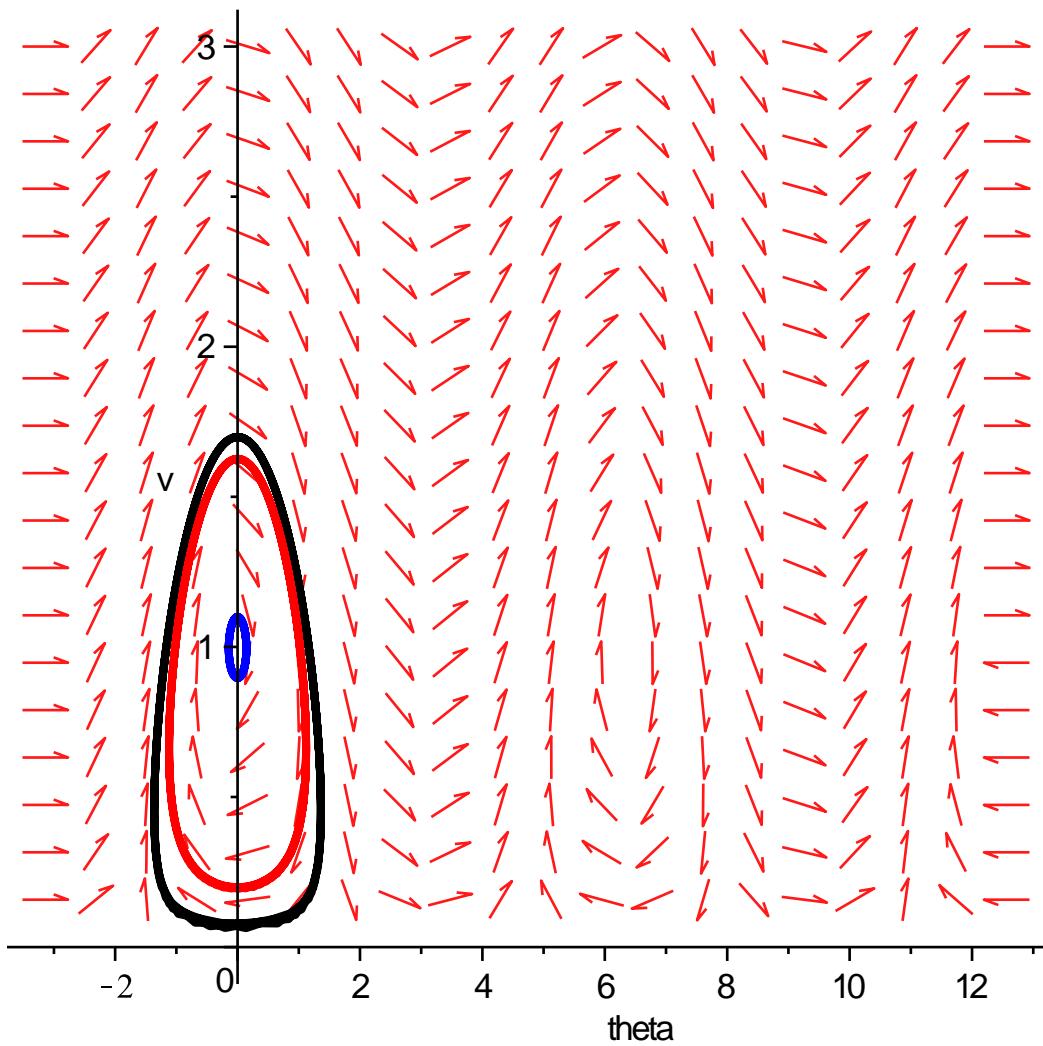
```



```
> DEplot( phug, [theta(t), v(t)], t=0..30,
  theta=-Pi..4*Pi, v=0..3,
  [[theta(0)=0, v(0)=1.7]],
  linecolor=[black], scene=[t,theta], view=[0..30,-2..2],
  stepsize=0.1);
```



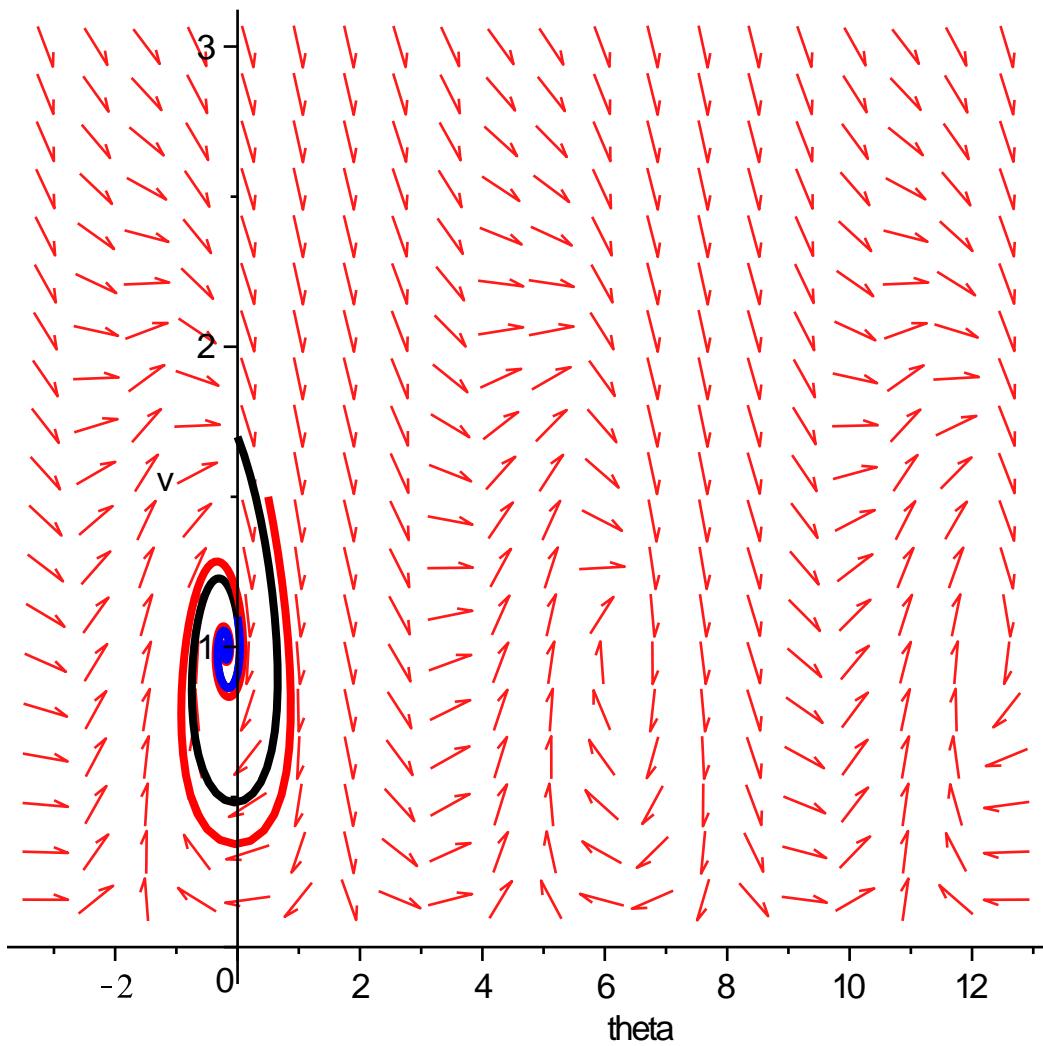
```
> R:=0;
DEplot( phug, [theta(t), v(t)], t=0..20,
theta=-Pi..4*Pi, v=0..3,
[[theta(0)=0, v(0)=1.7],[theta(0)=.5, v(0)=1.5], [theta(0)=0, v(0)=1.1]], stepsize=0.1,
linecolor=[black, red, blue]);
R := 0
```



```

> R:=0.2;
DEplot( phug, [theta(t), v(t)], t=0..20,
theta=-Pi..4*Pi, v=0..3,
[[theta(0)=0, v(0)=1.7],[theta(0)=.5, v(0)=1.5], [theta(0)=0, v
(0)=1.1]], stepsize=0.1,
linecolor=[black, red,blue]);
R := 0.2

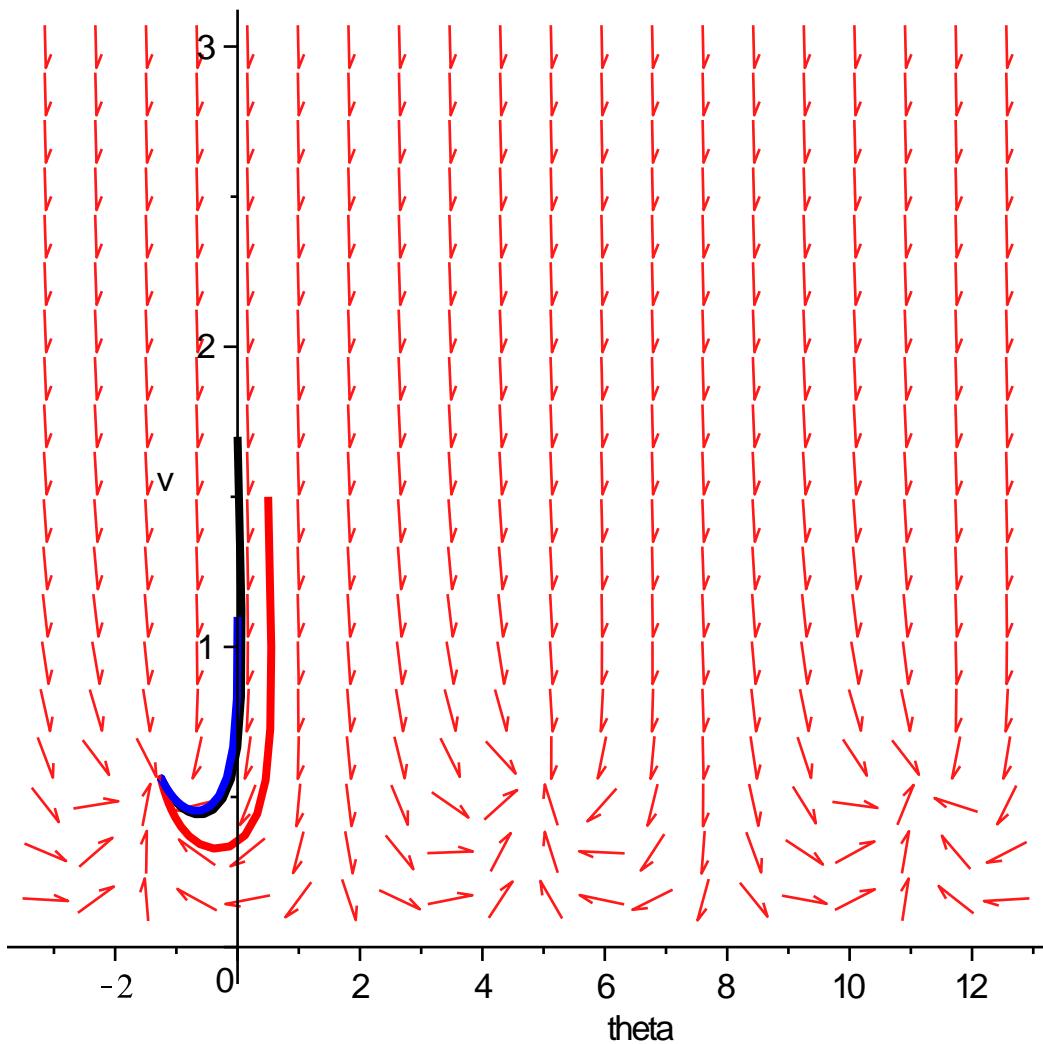
```



```

> R:=3;
DEplot( phug, [theta(t), v(t)], t=0..20,
theta=-Pi..4*Pi, v=0..3,
[[theta(0)=0, v(0)=1.7],[theta(0)=.5, v(0)=1.5], [theta(0)=0, v
(0)=1.1]], stepsize=0.1,
linecolor=[black, red,blue]);
R := 3

```



```

> R:=-0.1;
DEplot( phug, [theta(t), v(t)], t=-10..20,
theta=-Pi..4*Pi, v=0..3,
[[theta(0)=0, v(0)=1.7],[theta(0)=.5, v(0)=1.5], [theta(0)=0, v
(0)=1.1]], stepsize=0.1,
linecolor=[black, red,blue]);
R := -0.1

```

