

MAT331 homework problems

NOTE: Neither of these problems involve **Maple**, except as a word processor to write your solution. If you like, you are welcome to turn in a printed or handwritten version, if you are more comfortable with that.

11. (*expires 2/25*) Following Section 4 of the notes, prove that if we describe the circle of center (a, b) and radius r using the parameters (a, b, k) , with $k = a^2 + b^2 - r^2$, rather than the more natural parameters (a, b, r) , then the error function $H(a, b, k) = E(a, b, \sqrt{a^2 + b^2 - k})$ is quadratic in a, b and k . What does this imply about the number of critical points?
12. (*expires 2/25*) With reference to Problem #11, show that, for $r > 0$, the transformation $(a, b, r) \mapsto (a, b, k)$ is a valid change of variables, that is, it is one-to-one. This should help you prove that $E(a, b, r)$ has only one “physical” critical point, which is a minimum, and is mapped, through the transformation, into the unique critical point of $H(a, b, k)$.