

Your name: \_\_\_\_\_

TA's name: \_\_\_\_\_

Problem #1: Find the derivative of each function.

a)  $f(x) = \frac{3-\sqrt{x}}{3+\sqrt{x}}$

b)  $f(x) = (3x^2 + 9x - 4)(4x^3 + x^2 - x)$

Problem #2: Find the equation of the tangent line to  $y = \sin(4x)$  at  $x = \frac{\pi}{16}$ .

Problem #3: Find the  $x$ -values of the critical points of

$$y = x^3 - 6x^2 - 36x + 9.$$

Problem #4: Find  $\frac{dy}{dx}$  if  $x^3 - 5xy^2 + y^3 = 1$ .

Problem #5: Find the equation of the tangent line to  $\ln(2x^2 - y^2) = 0$  at  $(1,1)$ .

Problem #6: Find  $\frac{dy}{dx}$  if:

(a)  $y = \tan^{-1}(2x)$

this question uses material not on our exam that will appear on the final.

b)  $f(x) = \sin^3\left(\frac{2-5x}{x^2}\right)$

Problem #7: Find the points  $(x, y)$  where the line tangent to  $y = x^3 - 6x^2 - 30x + 4$  is parallel to  $15x + y = 10$ .

Problem #8: Find the values of  $x$  where  $y = x^2e^x$  has an absolute maximum or minimum on  $[-3,1]$ . Justify your answer.

This problem uses material we have not yet covered in class, and so won't be on our midterm.