

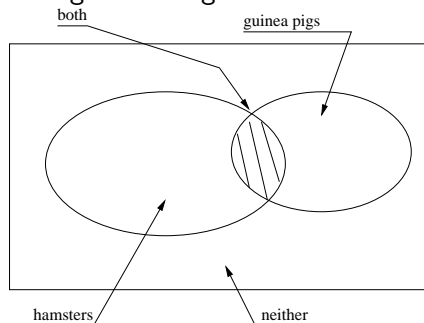
AMS 102: QUIZ 3

SOLUTIONS

In the town of Rodentville, half of the households own a hamster, 30% of all households own a guinea pig, and 35% of all households own neither a hamster, nor a guinea pig.

(a) Determine the percentage of households that own both a hamster and a guinea pig.

$100 - 35 = 65\%$ of households own either a hamster or a guinea pig. Therefore, $65\% = 50\% + 30\% - (\text{households that own both})$. Hence, 15% of households own both a hamster or a guinea pig. Alternatively you could use the following Venn diagram:



Hamsters and guinea pigs = 65%. Guinea pigs only = $65\% - \text{hamsters} = 65\% - 50\% = 15\%$.
Hamsters and guinea pigs = $30\% - 15\% = 15\%$.

(b) If you choose a Rodentville household at random, what is the probability that it owns a guinea pig?

30% or 0.3.

(c) Are the events “own a hamster” and “own a guinea pig” independent?

$P(\text{hamster}) = 0.5$, $P(\text{guinea pig}) = 0.3$, $P(\text{hamster AND guinea pig}) = 0.15$. Since $P(\text{hamster})P(\text{guinea pig}) = P(\text{hamster AND guinea pig})$, we conclude that the events are independent.

(d) The Johnsons own a guinea pig, while the Jacksons do not. Which household is more likely to own a hamster?

Neither. Since hamster ownership is independent of guinea pig ownership, knowing that a family owns/doesn't own one doesn't tell us anything about their chances to own the other.