

Long list of theorems for Final Exam

The topics listed here are recommended for review. One of them will be included (in a rephrased form) in the exam. It will be required to formulate the relevant definitions and theorems, but no proofs will be required. The word *section* means below a section from the textbook *Lessons in Geometry* by Jacques Hadamard, the words *Isometries* and *Similarity* refer to files *isometries.pdf* and *similarity.pdf*.

- (1) Theorem about vertical angles, section **12**.
- (2) Existence and uniqueness of perpendicular to a line from a point, section **19**.
- (3) Theorems about isosceles triangles and their properties, section **23**.
- (4) Tests for congruence of triangles, section **24**.
- (5) Triangle inequality and its corollaries, sections **26, 27**.
- (6) Bisector of an angle as the locus of point equidistant from the sides, section **36**.
- (7) Tests for parallel lines, section **38**.
- (8) Drawing through a given point a line parallel to a given line, section **39**.
- (9) Parallel Axiom, angles formed by parallel lines and transversal, sections **40, 41**.
- (10) The sum of interior angles in a triangle, section **44**.
- (11) Properties of a parallelogram, section **46, 46b, 47**.
- (12) Special types of parallelograms and their properties, section **48**.
- (13) Theorems about concurrent lines in a triangle, sections **52 - 54, 56**.
- (14) Theorem about a midline in a triangle, section **55**.
- (15) Existence and uniqueness of a circle passing through three points, section **57**.
- (16) Intersection of a line and a circle, section **58**.
- (17) Theorems about a diameter and a chord perpendicular to it, sections **61, 63**.
- (18) Theorems about an inscribed angle, section **73**.
- (19) Corollaries of the theorem about an inscribed angle, sections **74 -80**.
- (20) Constructions presented in sections **85 - 91, 93, 94**.
- (21) Recovering an isometry from its restriction to three points, Theorem 1 from *Isometries*.
- (22) Presentation of any plane isometry as a composition of at most three reflections, Theorem 2 from *Isometries*.
- (23) Types of isometries. Classification of plane isometries, Theorem 11 from *Isometries*.
- (24) Composition of two reflections, Theorem 7 from *Isometries*.
- (25) Thales' Theorem, sections **113** and **114**.
- (26) Properties of homotheties. A homothety as a similarity transformation, Theorems 1 and 2 from *Similarity*.
- (27) For angles, similarity is equivalent to congruence, Theorem 4 from *Similarity*.
- (28) Similarity tests for triangles, Theorems 5 - 7 from *Similarity*.
- (29) Theorem about a bisector, section **115**.
- (30) Geometric means in a right triangle, sections **123, 125**.
- (31) Pythagoras Theorem, section **124**.
- (32) Theorems about proportional segments in a circle, sections **131, 132**.
- (33) Radical axis of two circles, sections **126, 136, 137**.