

1. Reduce the expression $(x - 1 - i)(x - 1 + i)(x + 1 + i)(x + 1 - i)$ into the form $A + iB$.
2. Find real numbers x and y such that $(1 + 2i)x + (3 - 5i)y = 1 - 3i$.
3. Find a complex number z such that $(3 - 4i)z = 1 - 3i$.

4. Prove that $\left| \frac{z}{w} \right| = \frac{|z|}{|w|}$ for any complex numbers z and w with $w \neq 0$.

5. Given the system of equations

$$\begin{cases} (2 + i)x + (2 - i)y &= 6 \\ (3 + 2i)x + (3 - 2i)y &= 8. \end{cases}$$

(a) Find all its real solutions. (b) Find all its complex solutions.

6. Evaluate

(a) $\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^2$, (b) $\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^3$.

7. Describe the set of point which correspond to the complex numbers z satisfying the inequalities:

(a) $|z| < 2$, (b) $|z - i| \leq 1$.

Show these sets on pictures.

8. Show on a picture the set of points which correspond to the complex numbers z satisfying the following system of inequalities:

$$\begin{cases} 1 \leq z \cdot \bar{z} \leq 2 \\ -\sqrt{3} \leq \text{Im } z \leq 0. \end{cases}$$