

Sec. 1.9 2

$$A(\lambda) = \frac{1}{\pi} \int_{-\infty}^{\infty} f(x) \cos(\lambda x) dx = \frac{1}{\pi} \int_{t-h}^{t+h} \cos(\lambda x) dx = \frac{\sin(\lambda(t+h)) - \sin(\lambda(t-h))}{\pi}$$

$$B(\lambda) = \frac{1}{\pi} \int_{-\infty}^{\infty} f(x) \sin(\lambda x) dx = \frac{1}{\pi} \int_{t-h}^{t+h} \sin(\lambda x) dx = \frac{\cos(\lambda(t-h)) - \cos(\lambda(t+h))}{\pi}$$

So

$$f(x) = \int_{-\infty}^{\infty} A(\lambda) \cos(\lambda x) + B(\lambda) \sin(\lambda x) dx$$

Sec 1.11 2 First of all,

$$\frac{t}{4\pi} \sim 0.5 + \sum_{n=1}^{\infty} -\frac{\sin(\frac{n}{2}nt)}{n\pi}$$

Let

$$u(t) = A_0 + \sum_{n=1}^{\infty} A_n \cos(nt/2) + B_n \sin(nt/2),$$

Then by matching the coefficient, we get

$$A_0 = \frac{1}{2.08} A_n = \frac{0.4\pi}{(1.04 - n^2)^2 + (0.4n)^2} B_n = \frac{-1}{n\pi} \frac{1.04 - n^2}{(1.04 - n^2)^2 + (0.4n)^2} \quad (1)$$