

**MAT 319, SPRING 03**  
FOUNDATIONS OF ANALYSIS  
HOMEWORK SET # 1  
*Due Wednesday, February 5, 2003*

1. From section 1.1 of textbook do problems 1, 4, 5 and 23.
2. From section 1.2 do problems 1, 2, 4 and 6.
3. There exists a unique positive real number  $x$  that satisfies the algebraic equation

$$x^3 + x^2 - 5x - 5 = 0.$$

Later, we will be able to prove this assertion. At this time, express  $x$  as a Dedekind cut  $\alpha$ . Show that  $\alpha$  contains rationals  $> 2.236$  and list an increasing sequence of 20 such rationals. (Use of a calculator or MAPLE should simplify your calculations.)

4. From section 1.3 do problems 8, 10 and 17.
5. From section 1.4 do problems 1, 2, 5 and 15 .