MIDTERM 1					
MAT 142 10/07/05	Name	Sec.			
ID number			TA's name		
1	2	3	4	total	
	OU MAY USE	THE BACKS (OF PAGES FOI	RS IN THE SPACE R SCRATCH WORK	
			corresponding to answer is worth	o the correct answer in 2 points.	
$(\mathbf{a}) \ y =$		=	is one to one (one d) $y = x^2 + x^3$ (equal to $y = x^2 + x^3$	all real numbers)? e) $y = x + x^3$	
$(\mathbf{a}) f$	s bounded above			x > 0? x > 0 (c) $f(1) = 2$ (d)	
` '	- ' '	then its inverse (c) $\frac{1}{m}x + \frac{b}{m}$ (d)		$-\frac{m}{b}$ (f) none of these.	
	Evaluate $\int_0^{\pi/6} \tan \frac{1}{2}$ (b) $\ln 2$ (c) $\frac{1}{2}$ l) 2 ln 2 (f) none (of these.	
(v) (a) 30	Use Simpson's ru (b) $30\frac{1}{2}$ (c) $31\frac{3}{4}$	ule with $n = 4$ to (d) $31\frac{7}{8}$ (e) 32	approximate \int_0^2 (f) $32\frac{1}{12}$	$5x^4dx$.	
$\begin{array}{c} \overline{\text{of step}} \\ \mathbf{(a)} \ \int_0^1 \end{array}$	s) give the the ex	xact value?	Is does Simpson's $(\mathbf{d}) \int_1^2 \ln x dx$ (6)	rule (with any number e) $\int_0^1 \sqrt{x} dx$	

(viii)	Find the der (c) $2e^{2x} + (1+2x)$	ivative of $f(x) = e^{2x}$ (d) $2e^{2x} + 2(1)$	$(1+2x)e^{2x}$: (a) 2 $(1+2x)e^{2x}$ (e) $2e^{2x}$	$2(1+2x)e^{2x}$ (b)	$2xe^{2x}$ ese.
(ix)		iviative of $f(x) = \ln x \cos x$ (c) $x^{\cos x}$	$x^{\sin x}$: (a) $x^{\cos x}(\frac{1}{x})$	$\frac{1}{2}\cos x + \ln x \sin x$	
(x)	(f) none of these. If m, n are in (a) 0 (b) π (c) 0 i	ntegers then $\int_0^{2\pi} s$. If $n = m$ and π if	$ in(nx)\sin(mx)dx $ $ n \neq m (\mathbf{d}) 0 \text{ of } n $		$n \geq m$ (e)
ansv	π if $n=m$ and 0 if ots each, 10 pts were in the box. $\int \frac{1}{1+4x^2} dx,$			ntegrals. Put	your final

(ii) $\int_1^2 \frac{2}{x} \ln x dx,$	

(iii) $\int \frac{dx}{1+\cos x} dx$ (hint: multiply by 1),	

(iv)
$$\int_0^3 \frac{x^2 dx}{\sqrt{9-x^2}}$$
,

$$(v) \int_2^\infty \frac{dx}{(x-1)(x+1)},$$

- (3) (2 pts each, 10 pts total) (i) Expand using partial fractions: $\frac{x-1}{(x+1)^3}$.

(ii) Expand using partial fractions: $\frac{-2x+4}{(x^2+1)(x-1)^2}$.

For each of the following improper integrals, state whether the integral converges or diverges and explain why.

(iii)
$$\int_{1}^{\infty} x^{2} e^{-x} dx$$

(iv)
$$\int_0^1 \frac{x}{(1-x)^2} dx$$

(v)
$$\int_0^\infty \frac{dx}{(1+x)\sqrt{x}}$$

- (4) (5 pts each, 10 pts total): Do TWO of the following (your choice). Put your solutions on the following blank pages. Explain all your work. Put an "X" in the boxes corresponding to the two problems you want graded (choose at most 2):
 - (i) For which values of $0 does the integral <math>\int_0^\infty \frac{x^2}{x^p(1+x^p)} dx$ converge?
 - (ii) Use the definitions of \cosh , \sinh to prove $\cosh 2x = \cosh^2 x + \sinh^2 x$.
 - (iii) If n > 0 is an integer, evaluate $\int_0^{2\pi} [\sin(x) + \sin(2x) + \cdots + \sin(nx)]^2 dx$.
 - (iv) Which number is larger: 123456¹²³⁴⁵⁷ or 123457¹²³⁴⁵⁶?