

MAT 126 Fall 2020, Quiz 2

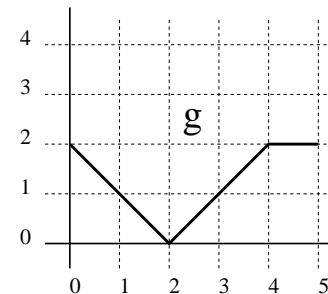
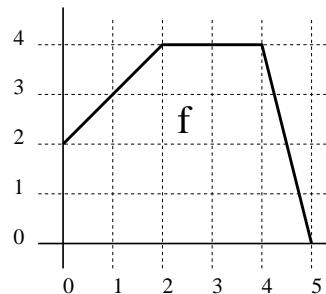
Name	ID	Section
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THIS QUIZ IS WORTH 10 POINTS. NO BOOKS, NOTES OR CALCULATORS ARE ALLOWED.

Write the correct answer in the box.

- (1)  Compute the integral  $\int_0^4 f(x)dx$  for the function plotted below.

- (a) 2
- (b) 4
- (c) 6
- (d) 10
- (e) 12
- (f) 14
- (g) 16
- (h) 18
- (i) 22
- (j) none of these



- (2)  Compute the integral  $\int_0^5 f(x) + g(x)dx$  using the functions plotted above.

- |        |        |        |
|--------|--------|--------|
| (a) -6 | (d) 4  | (g) 14 |
| (b) -2 | (e) 6  | (h) 18 |
| (c) 0  | (f) 10 | (i) 22 |
- (j) none of these

- (3)  Estimate the integral  $\int_0^4 f(x)g(x)dx$  using the function plotted above and left-hand rule with 4 intervals (use left endpoint of each subinterval).

- |       |       |        |
|-------|-------|--------|
| (a) 4 | (d) 7 | (g) 10 |
| (b) 5 | (e) 8 | (h) 11 |
| (c) 6 | (f) 9 | (i) 12 |
- (j) none of these

- (4)  Estimate the integral  $\int_1^5 f(g(x))dx$  using the functions plotted above and left-hand rule with 2 intervals.

- |       |       |        |
|-------|-------|--------|
| (a) 4 | (d) 7 | (g) 10 |
| (b) 5 | (e) 8 | (h) 11 |
| (c) 6 | (f) 9 | (i) 12 |
- (j) none of these

(5) Write down the integral that is represented by

$$\lim_{n \rightarrow \infty} \frac{2}{n} \sum_{k=1}^n \left(4 - \frac{4k^2}{n^2}\right)^{1/2}.$$

- |                                     |                                     |                                     |
|-------------------------------------|-------------------------------------|-------------------------------------|
| (a) $2 \int_0^1 \sqrt{4 - x^2} dx$  | (g) $\int_0^1 \sqrt{4 - x^2} dx$    | (m) $2 \int_0^1 \sqrt{4 - 2x^2} dx$ |
| (b) $4 \int_0^1 4 - 4x^2 dx$        | (h) $2 \int_0^1 4 - 4x^2 dx$        | (n) $2 \int_0^1 4 - 2x^2 dx$        |
| (c) $4 \int_{-1}^1 4 - 4x^2 dx$     | (i) $2 \int_{-1}^1 4 - 4x^2 dx$     | (o) $2 \int_{-1}^1 4 - 2x^2 dx$     |
| (d) $4 \int_0^1 \sqrt{4 - 4x^2} dx$ | (j) $2 \int_0^1 \sqrt{4 - 4x^2} dx$ | (p) none of these                   |
| (e) $2 \int_0^1 4 - x^2 dx$         | (k) $\int_0^1 4 - x^2 dx$           |                                     |
| (f) $2 \int_{-1}^1 4 - x^2 dx$      | (l) $\int_{-1}^1 4 - x^2 dx$        |                                     |

(6) Use geometry to evaluate the integral in part (5) and find the value of the limit.

- |              |           |             |                   |
|--------------|-----------|-------------|-------------------|
| (a) $2\pi/3$ | (d) 0     | (g) $2/3$   |                   |
| (b) $\pi$    | (e) $1/2$ | (h) 1       | (j) none of these |
| (c) $2\pi$   | (f) $1/4$ | (i) $\pi/4$ |                   |

**TRUE/FALSE:** put a T or F in each box.

(7)  The right hand rule gives a lower bound for  $\int_0^4 e^{-x} dx$ .

(8)  If  $a < b < c$  then  $\int_a^b f(x) dx + \int_b^c f(x) dx = 2 \int_a^c f(x) dx$ .

(9)   $\int_0^1 \frac{dx}{\sqrt{1+x}} \leq \int_0^1 \frac{dx}{\sqrt{1+x^2}}$ .

(10)   $\int_{-1}^1 x^{1001} e^{-x} dx > 0$ .

Answers: 1f, 2i, 3h, 4i, 5j, 6b, 7T, 8F, 9T, 10F