

# MAT 615: Complex Curves and Surfaces

## Problem Set 2

Written Solutions (if any) due by Wednesday, 03/01, 9:45am

*Please figure out all of the problems below and discuss them with others.*

**If you have not passed the orals yet, you are encouraged to write up concise solutions to problems adding up to 10 points in total.**

### Problem 1 (5 pts)

Describe all special divisors on a smooth compact Riemann surface of genus 0, 1 and 2.

### Problem 2 (5 pts)

Let  $C, D_1, D_2 \subset \mathbb{P}^2$  be smooth cubics so that

$$C \cdot D_1 = \sum_{i=1}^{i=9} p_i$$

as divisors on  $C$  and  $D_2$  passes through  $p_1, \dots, p_8$ . Show that  $p_9 \in D_2$ .

### Problem 3 (5 pts)

Let  $C \subset \mathbb{P}^n$  with  $n \geq 3$  be a smooth (connected) curve of genus 1 and degree 4. Show that  $C$  is contained in some linearly embedded  $\mathbb{P}^3 \subset \mathbb{P}^n$  and is the intersection of two quadric (degree 2) surfaces in that  $\mathbb{P}^3$ .