Math Club Problem of the Month (April 2010)

Find the 100-th derivative of the function

$$f(x) = \frac{x^2 + 1}{x^3 - x}$$