Math Club Problem of the Month (November 2009)

Let M be a square matrix consisting of 0's and 1's only. If there are precisely k 1's in each column, show that the determinant of M is divisible by k. Can the assumptions on the matrix be relaxed?