

$$2.1 A \quad (16) \quad \vec{q}_1 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}, \quad \vec{q}_2 = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \quad \vec{b} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\vec{b} = c_1 \vec{q}_1 + c_2 \vec{q}_2 \Leftrightarrow \begin{pmatrix} 0 \\ 1 \end{pmatrix} = c_1 \begin{pmatrix} 1 \\ 2 \end{pmatrix} + c_2 \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

$$\Leftrightarrow \begin{aligned} c_1 + 2c_2 &= 0 \Rightarrow c_1 = -2c_2 \\ 2c_1 + c_2 &= 1 \Rightarrow -4c_2 + c_2 = 1 \end{aligned} \quad \left. \begin{array}{l} c_1 = -2c_2 \\ -3c_2 = 1 \end{array} \right\}$$

$$\Rightarrow \begin{aligned} c_2 &= -\frac{1}{3} \\ c_1 &= -2c_2 = \frac{2}{3} \end{aligned} \quad \left. \begin{aligned} \left[\begin{pmatrix} 0 \\ 1 \end{pmatrix} &= \frac{2}{3} \begin{pmatrix} 1 \\ 2 \end{pmatrix} + -\frac{1}{3} \begin{pmatrix} 2 \\ 1 \end{pmatrix} \end{aligned} \right]$$

$$(18) \quad \vec{q}_1 = \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}, \quad \vec{q}_2 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, \quad \vec{q}_3 = \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$$

$$\vec{b} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} = c_1 \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} + c_2 \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} + c_3 \begin{pmatrix} 1 \\ 2 \\ 1 \end{pmatrix}$$

$$\Rightarrow \begin{aligned} c_2 + c_3 &= 1 \\ c_1 + c_2 + 2c_3 &= 2 \\ c_1 + c_3 &= 3 \end{aligned} \quad \left. \begin{array}{l} c_2 = 1 - c_3 \\ c_1 + 1 - c_3 + 2c_3 = 2 \\ c_1 + c_3 = 3 \end{array} \right\} \Rightarrow$$

$$\Rightarrow \text{eliminating } c_2 = 1 - c_3$$

$c_1 + c_3 = 1$ we see that these equations
 $c_1 + c_3 = 3$ contradict \Rightarrow no such coefficients exist.