

## 1 Problems

**Exercise 1.** You measure the distance to a tower to be 4 m. You turn through an angle of  $30^\circ$  and measure the distance to a different tower to be 8 m. How far are the towers?

**Exercise 2.** You have a triangle with angle  $A = 45^\circ$  and angle  $C = 60^\circ$ . The opposing side  $a$  to  $A$  has length 10. Find the length of the opposing side  $c$  to angle  $C$ .

**Exercise 3.** You have a triangle with angle  $A = 45^\circ$  and angle  $C = 30^\circ$ . The opposing side  $c$  to  $C$  has length 6. Find the length of the opposing side  $a$  to angle  $A$ .

**Exercise 4.** You have a triangle with angle  $A = 60^\circ$  and angle  $B = 45^\circ$ . The side opposite to  $B$  has length 16. Find the length of the side opposite to  $A$ .

**Exercise 5.** Compute  $\sin(\cos^{-1}(\frac{5}{13}))$ .

## 2 Answer key

**Exercise 1.**  $x = \sqrt{16 + 64(1 - \frac{\sqrt{3}}{2})}$

**Exercise 2.**  $c = \frac{10\sqrt{3}}{\sqrt{2}}$

**Exercise 3.**  $a = 6\sqrt{2}$ .

**Exercise 4.**  $x = \frac{16\sqrt{3}}{\sqrt{2}}$

**Exercise 5.**  $\frac{12}{13}$

## 3 Solutions

**Exercise 1.** Use the law of cosines:  $x^2 = 4^2 + 8^2 - 2 \cdot 4 \cdot 8 \cos(30^\circ) = 16 + 64 - 64(\frac{\sqrt{3}}{2}) = 16 + 64(1 - \frac{\sqrt{3}}{2})$ .  
So  $x = \sqrt{16 + 64(1 - \frac{\sqrt{3}}{2})}$ .

**Exercise 2.** Use the law of sines:  $\frac{\sin 45^\circ}{10} = \frac{\sin 60^\circ}{c}$ . Cross multiplying gives us  $c = \frac{10\sqrt{3}}{\sqrt{2}}$ .

**Exercise 3.** Use the law of sines:  $\frac{\sin 45^\circ}{a} = \frac{\sin 30^\circ}{6}$ . Cross multiplying gives us  $6\sqrt{2}$ .

**Exercise 4.** Law of sines:  $\frac{\sin 45^\circ}{16} = \frac{\sin 60^\circ}{x}$ . Solving for  $x$  gives us  $\frac{16\sqrt{3}}{\sqrt{2}}$ .

**Exercise 5.** By Pythagoras the remaining side of the triangle is 12. So we obtain  $\sin(x) = \frac{12}{13}$ .