

## Math 331, Fall 2002: Problems 7-10

**NOTE:** Each exercise is worth 10 points and can be turned in at any time before its “expiration date”. At the end of the semester, I will expect you to have turned in at least 2/5 of the exercises assigned. If you do more, I will pick your best grades. If you do less, the missing grades will be counted as zeros. Altogether, these will count the same as one project.

7. (*expires 9/30*) Fit the points  $(-1.9, -4.7), (-0.8, 1.2), (0.1, 2.8), (1.4, -1.2), (1.8, -3.5)$  by means of a quadratic function  $f(x) = ax^2 + bx + c$ , using the least square method. First, do this step by step, as we did in class; then, use the built-in **Maple** command, described in the notes. Check that the two solutions agree.

8. (*expires 9/30*) Fit the set of points

$$(1.02, -4.30), (1.00, -2.12), (0.99, 0.52), (1.03, 2.51), (1.00, 3.34), (1.02, 5.30)$$

with a line, using the least square method we used in class. You will see that this is not a good fit. Think of a better way to do the fit and use **Maple** to do it. Explain in your solution why you think your better way is better.

9. (*expires 10/7*) [*In this problem use **Maple** only as a word processor. If you're more comfortable with paper, you can turn in a paper instead of a **Maple** worksheet.*] Let  $n$  points of the form  $(r_i, r_i^2)$ ,  $i = 1, 2, \dots, n$ , be given. What is the quadratic function  $f(x) = ax^2 + bx + c$  that best fits them? **Prove** your answer. Does it depend on the optimization method (least square or others)?
10. (*expires 10/7*) Once we have calculated the line (or any other curve, for that matter) that best fits a sets of points, we can get an idea how good the fit is by plotting the line together with the points. It is much more scientific, however, to have a measure for this. Come up with a function of the data and parameters of a given best-fit problem that is small when the fit is good and large when the fit is bad, no matter how many points are used. Justify your answer.