

# MAT 126-Exam 1-Spring 2018

NAME: \_\_\_\_\_

TA NAME: \_\_\_\_\_

\*Each numbered question is worth 20 points.

1. For all parts in question #1  $f'(x) = \sqrt{9 - x^2}$

a.) Sketch a graph of  $f'$ .

b) Write an expression in sigma notation that represents the area under  $f'$  from  $x = 0$  to  $x = 3$ .

c) Find the exact value of the area under  $f'$  from  $x = 0$  to  $x = 3$ .

d) Sketch a graph of  $f$  if  $f(0) = 5$ .

2. Draw  $y = F(x) = \int_1^x (-1 + |t + 2|)dt$  with correct concavity on a scaled set of axes. (Include at least 3 labeled points.)

3. Use a left Riemann estimate with 2 subintervals to approximate the area between  $\frac{dy}{dx} = \sqrt{x^3 + 1}$  and the x axis from  $x = -1$  to  $x = 5$ . Now use this value to sketch  $y = f(x)$  if  $f(-1) = 2$

4) Compute the following for  $f(x) = \sin x + 2x$

$$a) \int_0^{2\pi} f(x) dx$$

$$b) \int_{2\pi}^0 f(x) dx$$

$$c) \lim_{n \rightarrow \infty} \frac{4\pi}{n} \sum_{i=1}^n f(x_i)$$

5. Using a right Riemann sum, compute the following using limits:

$$\int_1^3 x^2 dx$$