Another question:

Let $F(x, y) : \mathbb{R} \to \mathbb{R}$ satisfy $|F(x,y)| \leq \frac{1}{(1+x^2)(1+y^2)}$. Show (in detail) that

$$\lim_{N \to \infty} \lim_{M \to \infty} \int_{-N}^{N} \int_{-M}^{M} F(x,y)dxdy = \lim_{M \to \infty} \lim_{N \to \infty} \int_{-N}^{N} \int_{-M}^{M} F(x,y)dxdy$$

In particular, show that all four of the limits exist, and that you can change the order in which the limits are taken so that the right hand side and the left hand side are indeed equal.