MAT 150, Introduction to Advanced Mathematics
Homework 11, due by $11 / 29$
Name $\qquad$
Score $\qquad$

1. Find all ratonal solutions of the following equations:

$$
\begin{align*}
x^{2}+y^{2}+z^{2} & =1  \tag{1}\\
y^{3}+x^{2}-y^{2}+x z & =0 \tag{2}
\end{align*}
$$

2. Find all integer solutions of the equation $75 x-39 y=13$.
3. Construct a circle of a given radius $R$, which passes through a given point $A$ and is tangent to a given line $l$.
4. Construct a right isosceles triangle with hypotenuse connecting two given circles and the vertex with right angle at a given point.
5. Find the number of splitting of a natural number $S$ into a sum of $k$ natural numbers. The splittings which differ from each other by a permutation of summands are considered different.
