MAT 150, Introduction to Advanced Mathematics
Homework 10, due by $11 / 17$

Name $\qquad$
Score $\qquad$

1. Let $A$ and $B$ be two points on the plane, and let $l$ and $m$ be parallel lines separating $A$ from $B$. Find the shortes broken line connecting $A$ to $B$ and having the segment between $l$ and $m$ perpendicular to $l$. (If $l$ and $m$ are the shores of a river, where to make the shortest road between vallages $A$ and $B$ crossing the river with a bridge perpendicular to the shores.)
2. Given circles $b$ and $c$ which have a common point $A$. Find a line $l$ which passes through $A$ and cut congruent chords $A B$ and $A C$ on the circles $b$ and $c$.
3. Find all rational solutions of the equation $y^{3}=x^{2}-y^{2}$.
4. How to detect whether it is possible to draw a given planar graph (i.e., a network of arcs on the plane) without passing any of the arcs twice and without raising the pen?
