

Sec. 2.1 2 It is easy to see

$$\frac{\partial^2}{\partial^2 x}(e^{-\lambda^2 kt} \cos(\lambda x)) = -\lambda^2 e^{-\lambda^2 kt} \cos(\lambda x)$$

$$\frac{\partial^2}{\partial^2 x}(e^{-\lambda^2 kt} \sin(\lambda x)) = -\lambda^2 e^{-\lambda^2 kt} \sin(\lambda x)$$

$$\frac{\partial}{\partial t}(e^{-\lambda^2 kt} \cos(\lambda x)) = -k\lambda^2 e^{-\lambda^2 kt} \cos(\lambda x)$$

$$\frac{\partial}{\partial t}(e^{-\lambda^2 kt} \sin(\lambda x)) = -k\lambda^2 e^{-\lambda^2 kt} \sin(\lambda x)$$

So we get the desired equality.