MAT514 - Analysis for Teachers II - Summer II 2019

Potential Project and Presentation Ideas.

- 1. As many proofs as you can find of the Fundamental Theorem of Algebra.
- 2. Harmonic Functions
- 3. Conic Sections using complex analysis
- 4. The maximum modulus principle and the open mapping theorem for holomorphic functions.
- 5. Conformal Mapping and The Riemann Mapping Theorem
- 6. The Schwarz-Christoffel Formula and the Riemann mapping theorem
- 7. Complex Dynamics: Iteration of polynomials $z^2 + c$ and the Mandelbrot set.
- 8. Green's theorem and Cauchy's Theorem
- 9. The hyperbolic disk and upper half plane.
- 10. Interesting applications of the Residue Theorem.
- 11. Proof of the Cauchy Integral Formula.
- 12. The Prime Number Theorem.
- 13. Proof of a function with zero derivative being a constant.
- 14. Proofs from Real Analysis made easy by complex analysis.
- 15. Notions of Complex Analysis that appear in NYS high school math syllabi.
- 16. Goursat's Theorem.
- 17. Taylor's theorem and a converse to the Cauchy Riemann equations.
- 18. The concept of homotopy and how it relates to Cauchy's Theorem.
- 19. Solving for the zeros of a cubic, quartic, and quintic polynomial.
- 20. Program interesting software to help visualize any of the concepts in class.
- 21. Applications of complex variables to physical or engineering problems.