

MAT 541
ALGEBRAIC TOPOLOGY I

Instructor: Blaine Lawson

Office: 5-109.

Office Hours: Tu.-Thur. 11:30-1:00 or by appointment (just e-mail or speak to me).

References:

Algebraic Topology, by A. Hatcher

Algebraic Topology , a First Course (revised), by M. Greenberg and J. Harper

Lectures on Algebraic Topology, by A. Dold

Algebraic Topology, by E. Spanier

A Concise Course in Algebraic Topology, by J. P. May

Elements Of Algebraic Topology, by J. Munkres

Differential Forms in Algebraic Topology, by R. Bott and L. Tu

Algebraic Topology from a Homotopical Viewpoint, Aguilar, Gitler, and Prieto

Lectures Tues.-Thurs. 10:00-11:20 in Physics P122

Homework will be due every two weeks. Each time just hand in three of the problems that I have mentioned in class.

SYLLABUS

1. Some Basic Homotopy Theory:

- Basic Concepts and Examples
- Suspension and Loop Spaces
- Higher Homotopy Groups and some properties
- Relative Groups and the Long Exact Sequence
- CW-Complexes
- Fibrations and Fibre Bundles
- The Long Exact Sequence for a Fibration

2. Homology:

- Singular Homology Theory
- Homotopy Invariance
- The Exact Homology Sequence
- Excision
- Mayer-Vietoris Sequence
- Cell Complexes
- The Hurewicz Theorem
- The Whitehead Theorem

- Axioms
3. Cohomology:
 - Singular Cohomology and Cohomology with Compact Supports.
 - The Universal Coefficient Theorem
 - $K(\pi, n)$ -Spaces
 4. Products:
 - The Cup Product
 - The Cap Product
 5. Dualities
 - Poincaré Duality
 - Alexander Duality
 - Lefschetz Duality
 6. (If there is time) Differential Characters or Cohomology Operations

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