

# **MAT 566: Differential Topology**

## **Spring 2018**

### **Presentation 5: Atiyah-Singer Index Theorem** **(after Multiplicative Sequences)**

You should give an indication of what the Index Theorem is about and perhaps of where it comes from based on Chapter 3 of *Spin Geometry*:

- (1)  $A$ -class in general, as well as for smooth complex curves and surfaces;
- (2) statements of the Index Theorems;
- (3) some examples such as Riemann-Roch for a curve, Noether's Lemma, Euler class formula, Signature Theorem;
- (4) a little bit of where the Index Theorem comes from, such as pseudodifferential operators and  $K$ -theory