

MATH 126

Second Midterm

Thursday March 25, 2010

Name: _____ ID: _____ Rec: _____

Question:	1	2	3	4	5	6	Total
Points:	30	45	45	45	45	40	250
Score:							

There are 6 problems in this exam, printed on 6 pages (not including this cover sheet). Make sure that you have them all.

Do all of your work in this exam booklet, and cross out any work that the grader should ignore. You may use the backs of pages, but indicate **clearly** what is where if you expect someone to look at it. **Books, calculators, extra papers, and discussions with friends are not permitted.** Leave all answers in exact form (that is, do *not* approximate π , square roots, and so on.)

If you wish to use your psychic abilities to read the proctor's mind for the answers, you may do so. However, remember that he may be deliberately thinking of the *wrong* answers during the test.

You must give a correct justification of all answers to receive credit.

You have 90 minutes to complete this exam.

Name: _____

Id: _____

1. Determine these EASY antiderivatives. You should be able to do these **very well**. In these problems, no justification is needed. Remember the '+C'.

6 pts

(a) $\int \frac{2}{x} dx$

6 pts

(b) $\int 2 \sin(x) dx$

6 pts

(c) $\int e^{4x} dx$

6 pts

(d) $\int \frac{2}{t^2 + 1} dt$

6 pts

(e) $\int \frac{1}{\sqrt{1 - u^2}} du$

Name: _____

Id: _____

2. In this question we tell you which method we suggest you use. Use the back of the previous page if you need more space.

15 pts

(a) Suggested method: substitution $\int \frac{y}{1+y^2} dy$

15 pts

(b) Suggested method: substitution $\int \frac{e^{\sqrt{x+1}}}{\sqrt{x+1}} dx$

15 pts

(c) Suggested method: substitution $\int \frac{\ln(z)}{z} dz$

Name: _____

Id: _____

3. In this question we tell you which method we suggest you use. Use the back of the previous page if you need more space.

15 pts

(a) Suggested method: integration by parts $\int x^6 \ln(x) dx$

15 pts

(b) Suggested method: integration by parts $\int xe^{2x} dx$

15 pts

(c) Suggested method: integration by parts $\int \sin(x)e^{3x} dx$

Name: _____

Id: _____

4. Determine the following antiderivatives. Use the back of the previous page if you need more space.

15 pts

(a) $\int \sin^3(x) dx$

15 pts

(b) $\int \frac{1}{\sec(2x)} dx$

15 pts

(c) $\int \frac{1}{x^2\sqrt{x^2-1}} dx$

Name: _____

Id: _____

5. Evaluate these definite integrals. Use the back of the previous page if you need more space.

15 pts

(a) $\int_{-\frac{1}{2}}^{\frac{1}{2}} \frac{1}{1-x^2} dx$

15 pts

(b) $\int_{-100}^{100} \frac{\sin^{21}(x)}{1+e^{x^2}} dx$

15 pts

(c) $\int_0^1 \frac{x}{\sqrt{4-x^2}} dx$

Name: _____

Id: _____

6. Since $\int_0^1 \frac{1}{1+x^2} dx = \arctan(1) = \frac{\pi}{4}$, evaluating the integral $\int_0^1 \frac{4}{1+x^2} dx$ gives π .

20 pts

(a) Use Simpson's rule with 2 intervals to estimate $\int_0^1 \frac{4}{1+x^2} dx$.

20 pts

(b) How many intervals are needed to estimate $\int_0^1 \frac{4}{1+x^2} dx = \pi$ within .0001 using the trapezoid rule?¹

¹Use the following estimate for E_T using n intervals: If $|f''(x)| \leq K$ then $E_T \leq K \frac{(b-a)^3}{12n^2}$.

If $f(x) = \frac{1}{1+x^2}$, then $f''(x) = \frac{6x^2 - 2}{(1+x^2)^3}$