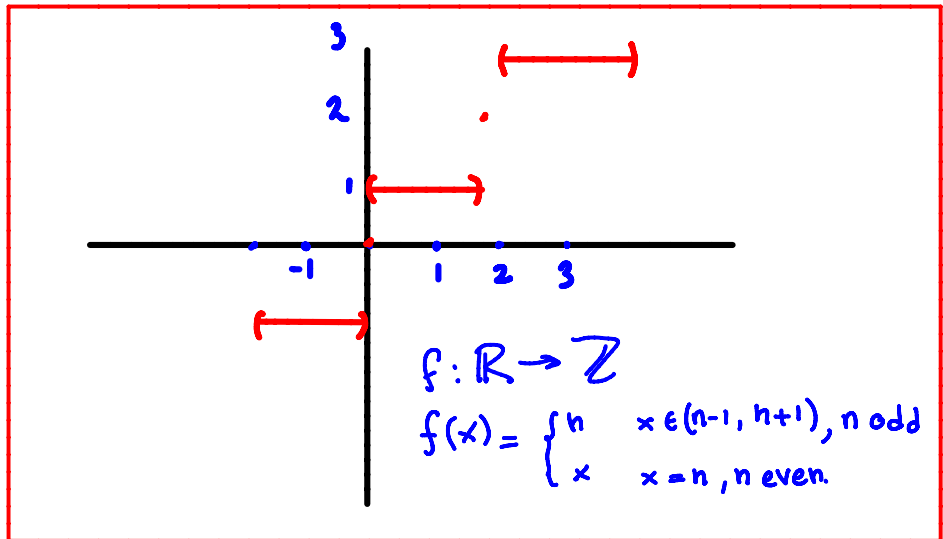


Find the quotient topology.

$$\textcircled{1} \quad X = \{\alpha, \beta, \gamma\}$$

$$f: \mathbb{R} \rightarrow X$$

$$f(x) = \begin{cases} \alpha & x < 0 \\ \beta & x = 0 \\ \gamma & x > 0 \end{cases}$$



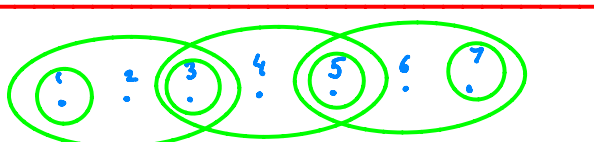
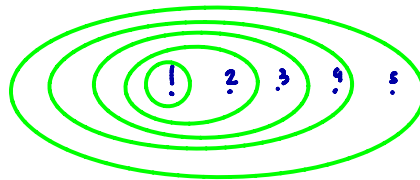
$$f: [0, 4] \rightarrow \{0, 1, 2, 3, 4\}$$

$$f(x) = \begin{cases} \lfloor x \rfloor, & x \in [0, 2) \\ \lceil x \rceil, & x \in (2, 4] \\ 2 & x = 2 \end{cases}$$

where $\lfloor x \rfloor$ is the largest integer smaller than x
 $\lceil x \rceil$ is the smallest integer larger than x

$$f: \{1, 2, 3, 4, 5\} \rightarrow \{a, b\}$$

$$f(x) = \begin{cases} a & x \leq 2 \\ b & x \geq 3 \end{cases}$$



$$f: \{1, 2, 3, 4, 5, 6, 7\} \rightarrow \{1, 2, 3, 4, 5, 6\}$$

$$f(x) = \begin{cases} x & x \leq 6 \\ 1 & x = 7 \end{cases}$$

$$f: [0,1] \rightarrow A$$

$$A = (0,1) \cup \{p\}$$

$$f(x) = \begin{cases} x & x \in (0,1) \\ p & x=0 \text{ or } x=1 \end{cases}$$

$$f: [0,1] \times [0,1] \rightarrow A$$

$$A = (0,1) \times [0,1] \cup \{p\} \times [0,1]$$

$$f(x) = \begin{cases} x & x \in (0,1) \times [0,1] \\ (p, \pi) & x = (0, \pi) \text{ or } (1, \pi) \end{cases}$$

A is the following partition of $[0,1] \times [0,1]$

$$A = \{(x,y)\}_{(x,y) \in \mathbb{R}^2} \cup \{(0,y), (1,y)\}_{y \in (0,1)} \\ \cup \{(x,0), (x,1)\}_{x \in (0,1)} \cup \{(0,0), (0,1), (1,0), (1,0)\}$$

$$f: [0,1] \times [0,1] \rightarrow A \\ (x,y) \rightarrow \text{subset of } A / (x,y) \in C$$

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$$f: [0,1] \times [0,1] \rightarrow A \\ (x,y) \rightarrow \text{subset of } A / (x,y) \in C$$

$$A = \{0,1,2,3\} \cup \{x\}_{x \in (0,1) \cup (2,3)}$$

$$[0,1] \cup [2,3] \rightarrow A$$

$$x \rightarrow \text{subset of } A \text{ containing } x$$

$$A = \{0,1,2,3,4\} \cup \{x\}_{x \in (0,1) \cup (2,3)}$$

$$[0,1] \cup [2,3] \cup [4,5] \rightarrow A$$

$$x \rightarrow \text{subset of } A \text{ containing } x$$