Homework 2

- (1) Construct a simplicial complex homeomorphic to the
 - (a) 2-sphere and
 - (b) the 2-torus

and compute the resulting homology groups.

- (2) (Munkres, Chapter 6 exercise 7).
 - Construct a simplicial complex homeomorphic to the 'dunce cap' given by the pentagon with its sides identified as follows:



A

Now compute its homology.

- Do the same thing when the 5-gon above is replaced by an *n*-gon.
- (3) (Munkres Chapter 6, exercise 8.)

Let G_1 and G_2 be finitely generated abelian groups, where G_2 is free. Construct a simplicial complex whose *p*th homology group is G_p for p = 1, 2.

(4) Compute the homology of the boundary of an n-simplex.

Hint: Use the fact that the reduced homology of an *n*-simplex is vanishes.