## Corrections to Advanced Algebra‘ Digital Second Edition

Page 451, line -7. Insert the following sentence after the word "Remarks": "Corollary 8.21 of Basic Algebra shows that $A[X]$ is a unique factorization domain."

Page 452, line 7. Change "But" to "Since".
Page 452, line 8. Delete "and thus".
Page 452, line 9. Insert "by Corollary 8.21 of Basic Algebra" after "domain" and before the comma.

Page 453, line 4. Change "statement" to "statements".
Page 453 , line -3 of the top proof. Insert the following sentence right before "If both": "This proves existence of $a$ and $b$."

Page 453, end of top proof. Insert an additional paragraph before the end-of-proof symbol, as follows: "For uniqueness of $a$ and $b$ when $R(f-g) \neq 0$, suppose there are two distinct pairs $(a, b)$ with $a f+b g=R$. Taking the difference of the two equations leads to an equation $a f+b q=0$ with $\operatorname{deg} a<n$ and $\operatorname{deg} b<m$. The implication that (b) implies (c) shows that $R(f, g)=0$, and this conclusion contradicts the assumption that $R(f, g) \neq 0$.

Page 454, line 4 of the large bracketed display in the middle. Change "with $i \leq n^{\prime}+j \leq$ $m^{\prime}+i$ " to "with $i \leq n^{\prime}+j \leq n^{\prime}+i$ ".
Page 456 , last line of Section 2. Change " $(h) \subseteq(f) \cap(g)$ " to " $(h) \supseteq(f) \cap(g)$ ".
Page 466, line 2. Change "Consequently" to "Since $y_{i} X-x_{i} Y$ is irreducible in $K[X, Y]$, the principal ideal $\left(y_{i} X-x_{i} Y\right)$ is prime, and Corollary 7.2 of the Nullstellensatz shows that".

Page 492, line -5 . In the display in the example, change the term " $2 X Y$ " to " $2 X Y^{2}$ ".
Page 500 , line -6 . A set of parentheses is missing around the rightmost $f_{j}$ in the middle member of the displayed inequalities. Change the middle member so that it reads $" \max \left(\operatorname{LM}\left(a_{j} f_{j}\right), \operatorname{LM}\left(\operatorname{LT}(p) / \operatorname{LT}\left(f_{j}\right)\right) \operatorname{LM}\left(f_{j}\right)\right) "$.
Page 501, lines $1-2$. Replace "Since $\operatorname{Lm}(p)=\operatorname{LM}(\operatorname{LT}(p))$, Proposition 8.18 shows that $\operatorname{LM}(p)$ strictly decreases" by "Since $\operatorname{LT}(p)=\operatorname{LT}(\operatorname{LT}(p))$, Proposition 8.18 shows that $\operatorname{LM}(p-\operatorname{LT}(p))<\operatorname{LM}(p)$, and thus $\operatorname{LM}(p)$ strictly decreases".
Page 501, line -10 . Change " $\operatorname{LM}(I) "$ to " $\operatorname{LT}(I)$ ".
Page 504, line -1 . Change " $\sum_{j, k}$ " on the right side to " $\sum_{j<k}$ ".
Page 506, line -10 of text. Change " 8.23 c " to " 8.23 b ".
Page 508 , line 2 of the remark with Lemma 8.27. Change " $j \geq 1$ " to " $j \geq 2$ ".
Page 509, lines -14 and -13 . Change "We conclude that $k=i$ and that $\operatorname{LM}\left(h_{i}\right)=$ $\operatorname{LM}\left(g_{i}=h_{i}\right)$ " to "We conclude that $k=i$. The divisibility in $(*)$ then implies that $\operatorname{LM}\left(h_{i}\right) \leq \operatorname{LM}\left(g_{i}-h_{i}\right) . "$
Page 510, second display. Change $"="$ to $" \geq$ ".
Page 512, line -4 . Change " $a_{i} f_{i}$ " to " $a_{i} g_{i}$ ".
Page 513 , line 4 . In the second term of the right member of the displayed equality, change the numerator of the fraction from " $\operatorname{LCM}\left(\operatorname{LM}\left(g_{k}\right), \operatorname{LM}\left(g_{k}\right)\right) "$ to $" \operatorname{LCM}\left(\operatorname{LM}\left(g_{j}\right), \operatorname{LM}\left(g_{k}\right)\right)$ ".
Page 513, lines 5-6. Change "since the monomial ordering is of $k$-elimination type" to "since $g_{1}, \ldots, g_{t}$ by construction are all in $K\left[X_{k+1}, \ldots, X_{n}\right]$ ".
Page 513 , line -15 . Change " $4^{\text {th } " ~ t o ~ " ~} 3^{\text {rd } " . ~}$
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